

# 1295. Crazy Notions

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$$1^2 + 2^2 + 3^2 + 4^2 + \dots$$

How much zeros does its decimal notation end with?

100 answer is 2

640 answer is 1

999 answer is 0

## Input

The only line contains an integer  $n$  ( $1 \leq n \leq 300000$ ).

## Output

Output the number of zeroes the decimal notation of  $1^n + 2^n + 3^n + 4^n$  ends with.

### Samples

input	output
1	1
3	2

## My first attempt

```
1  n = input()
2
3  x = 1**int(n) + 2**int(n) + 3**int(n) + 4**int(n)
4
5  arr = list(str(x))
6
7  count = 0
8  for i in range(len(arr)-1,-1,-1):
9      |   if arr[i] == '0':
10     |       |   count += 1
11     |   else:
12     |       |   break
13
14  print(count)
```

# Running Time of My first attempt

$$2^{**}n = \underbrace{2^*2^*2^* \dots\dots\dots 2}_{n}$$

$$2^{**}n + 3^{**}n + 4^{**}n = 3n$$

```
1  from time import time
2
3  n = 1000000
4
5  x = 2**n
6  y = 3**n
7
8  start = time()
9  print(x+y)
10
11 end = time()
12
13 print("time:",end-start)
```

$$2^{**}n + 3^{**}n$$

$$n = 1000000$$

$$n = 100000$$

```
369385748873959648658182738283436617900770000600931379426158877713  
099427265183032299511930882689573149205637715923028682912652024874  
480878785688594572122782107449889186870829664812138695809058058586  
77  
time: 6.886989593505859  
320853458911950460112424860475  
time: 0.08600139617919922
```

# Thank you for hint

Posted by [Md. Shahedul Islam \(Shahed\)](#) 13 Aug 2015 15:15

if  $\{(1^n + 2^n + 3^n + 4^n) \% 10\}$  is equal to 0, then we find 1 zero.  
if  $\{(1^n + 2^n + 3^n + 4^n) \% 100\}$  is equal to 0, then we find 2 zeros.  
and so on....

now, how to calculate  $\{(1^n + 2^n + 3^n + 4^n) \% 10\}$ :

Look,  
 $\{(1^n + 2^n + 3^n + 4^n) \% 10\}$   
 $=((1^n \% 10) + (2^n \% 10) + (3^n \% 10) + (4^n \% 10)) \% 10$  [simple modulo equivalencies]

now,  
 $(4^n \% 10)$   
 $= ((((((4 \% 10) * 4) \% 10) * 4) \% 10) * 4) \% 10 \dots (n \text{ times})$  [ $(4 \% 10)$ , then multiply by 4, then mod 10, loop for n times]  
similarly for  $(2^n \% 10)$  and  $(3^n \% 10)$ . No need for 1, because  $(1^n \% 10)$  is always 1.

In this way, calculate the result of  $\{(1^n + 2^n + 3^n + 4^n) \% m\}$  for  $m = 10, 100$ , ans so on... and count zeros... :)

```
1 n = input()
2
3 cal1 = cal2 = cal3 = cal4 = 1
4
5 for i in range(int(n)):
6     cal2 = (cal2*2)%100
7     cal3 = (cal3*3)%100
8     cal4 = (cal4*4)%100
9
10 x = cal1+cal2+cal3+cal4
11
12 arr = list(str(x))
13
14 count = 0
15 for i in range(len(arr)-1,-1,-1):
16     if arr[i] == '0':
17         count += 1
18     else:
19         break
20
21 print(count)
```

	Language	Judgement result	Test #	Execution time	Memory used
	Python 3.6	Accepted		0.327	304 KB

$$2^{**}2 = 4$$

$$2^{**}22 = \dots 04$$

$$3^{**}1 = 3$$

$$3^{**}21 = \dots 03$$

22

n = 0 2

n = 0 3

n = 0 4

n = 1 4

n = 1 9

n = 1 16

n = 21 4

n = 21 9

n = 21 16