

1295. Crazy Notions

Tanapat L. 6014216
Aung Hlaing Moe 5745402

$$1^M + 2^M + 3^M + 4^M$$

How much zeros does its decimal notation end with?

100 answer is 2

640 answer is 1

999 answer is 0

Input

The only line contains an integer n ($1 \leq n \leq 300000$).

Output

Output the number of zeroes the decimal notation of $1^n + 2^n + 3^n + 4^n$ ends with.

Samples

input	output
1	1
3	2

My first attempt

```
1  n = input()
2
3  x = 1**int(n) + 2**int(n) + 3**int(n) + 4**int(n)
4
5  arr = list(str(x))
6
7  count = 0
8  for i in range(len(arr)-1,-1,-1):
9      if arr[i] == '0':
10         count += 1
11     else:
12         break
13
14  print(count)
```

Running Time of My first attempt

$$2^{**}n = \underbrace{2*2*2*.....2}_n$$

$$2^{**}n + 3^{**}n + 4^{**}n = 3n$$

```
1  from time import time
2
3  n = 1000000
4
5  x = 2**n
6  y = 3**n
7
8  start = time()
9  print(x+y)
10
11 end = time()
12
13 print("time:",end-start)
```

$$2^{**}n + 3^{**}n$$

$$n = 1000000$$

$$n = 100000$$

```
369385748873959648658182738283436617900770000600931379426158877713
099427265183032299511930882689573149205637715923028682912652024874
480878785688594572122782107449889180870829664812138695809058058586
77
time: 6.886989593505859
320853458911950460112424860475
time: 0.08600139617919922
```

Thank you for hint

Posted by [Md. Shahedul Islam \(Shahed\)](#) 13 Aug 2015 15:15

if $\{(1^n + 2^n + 3^n + 4^n) \% 10\}$ is equal to 0, then we find 1 zero.
if $\{(1^n + 2^n + 3^n + 4^n) \% 100\}$ is equal to 0, then we find 2 zeros.
and so on....

now, how to calculate $\{(1^n + 2^n + 3^n + 4^n) \% 10\}$:

Look,
 $\{(1^n + 2^n + 3^n + 4^n) \% 10\}$
 $= ((1^n \% 10) + (2^n \% 10) + (3^n \% 10) + (4^n \% 10)) \% 10$ [simple modulo equivalencies]

now,
 $(4^n \% 10)$
 $= ((((((4 \% 10) * 4) \% 10) * 4) \% 10) * 4) \% 10 \dots (n \text{ times})$ $[(4 \% 10), \text{ then multiply by 4, then mod 10, loop for } n \text{ times}]$
similarly for $(2^n \% 10)$ and $(3^n \% 10)$. No need for 1, because $(1^n \% 10)$ is always 1.

In this way, calculate the result of $\{(1^n + 2^n + 3^n + 4^n) \% m\}$ for $m = 10, 100$, and so on... and count zeros... :)

```

1  n = input()
2
3  cal1 = cal2 = cal3 = cal4 = 1
4
5  for i in range(int(n)):
6      cal2 = (cal2*2)%100
7      cal3 = (cal3*3)%100
8      cal4 = (cal4*4)%100
9
10 x = cal1+cal2+cal3+cal4
11
12 arr = list(str(x))
13
14 count = 0
15 for i in range(len(arr)-1,-1,-1):
16     if arr[i] == '0':
17         count += 1
18     else:
19         break
20
21 print(count)

```

	Language	Judgement result	Test #	Execution time	Memory used
	Python 3.6	Accepted		0.327	304 KB

$$2^{**}2 = 4$$

$$2^{**}22 = \dots 04$$

$$3^{**}1 = 3$$

$$3^{**}21 = \dots 03$$

22

$n = 0 \quad 2$

$n = 0 \quad 3$

$n = 0 \quad 4$

$n = 1 \quad 4$

$n = 1 \quad 9$

$n = 1 \quad 16$

$n = 21 \quad 4$

$n = 21 \quad 9$

$n = 21 \quad 16$